

Investigating the impact of Data Monitoring Committee recommendations on the probability of trial success

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Hybrid Bayesian/frequentist design of a superiority phase III trial

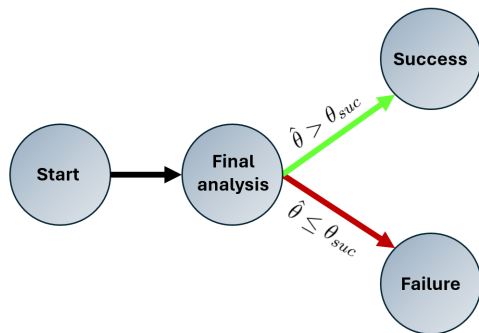
θ is the treatment effect (e.g., mean treatment difference between T and R)

Success is defined as rejecting H_0 (e.g., $H_0 : \theta \leq 0$)

$q_0(\theta)$ is the prior distribution of the treatment effect

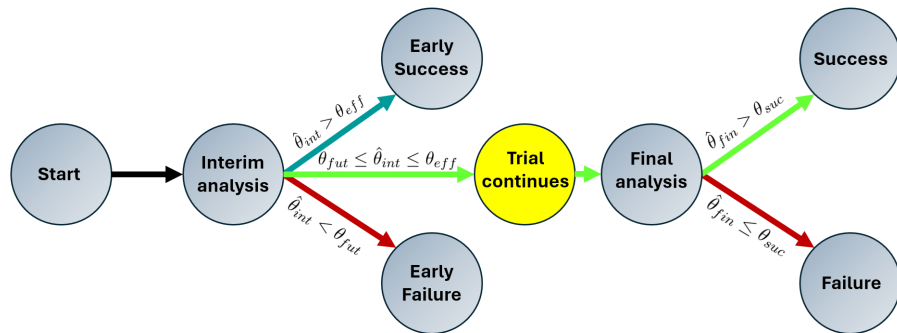
\Rightarrow used to compute the **Probability of Success** (*PoS*)

PoS in a one-stage clinical trial



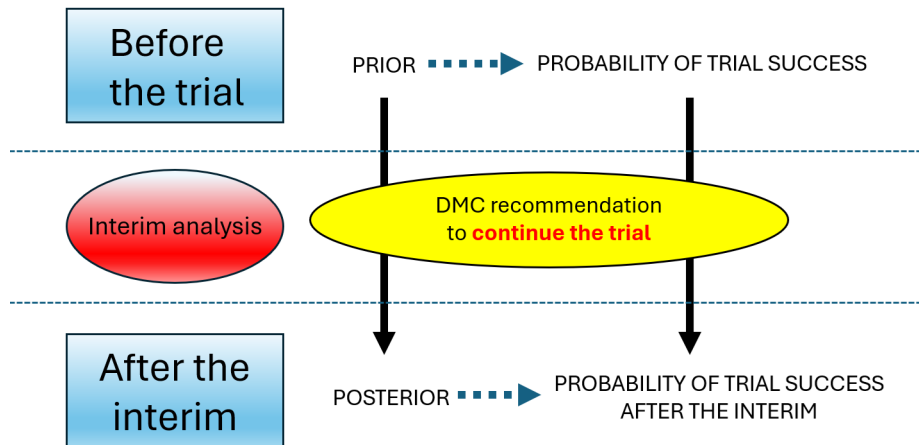
$$PoS = P(\text{trial success}) = \int P(\hat{\theta} > \theta_{suc} | \theta) q_0(\theta) d\theta$$

PoS in a two-stage clinical trial



$$\begin{aligned} PoS &= P(\text{early stop for efficacy}) + P(\text{no early stop and success at final analysis}) \\ &= \int P(\hat{\theta}_{int} > \theta_{eff} | \theta) q_0(\theta) d\theta + \int P(\theta_{fut} \leq \hat{\theta}_{int} \leq \theta_{eff}, \hat{\theta}_{fin} > \theta_{suc} | \theta) q_0(\theta) d\theta \end{aligned}$$

Incorporating DMC recommendation to continue the trial



PoS post interim

PoS is updated using the information $\theta_{fut} \leq \hat{\theta}_{int} \leq \theta_{eff}$:

$$PoS_{post} = \int P(\hat{\theta}_{fin} > \theta_{suc} | \theta_{fut} \leq \hat{\theta}_{int} \leq \theta_{eff}, \theta) q_1(\theta) d\theta$$

where $q_1(\theta)$ is the posterior:

$$q_1(\theta) = \frac{P(\theta_{fut} \leq \hat{\theta}_{int} \leq \theta_{eff} | \theta) q_0(\theta)}{\int P(\theta_{fut} \leq \hat{\theta}_{int} \leq \theta_{eff} | \theta') q_0(\theta') d\theta'}$$

Relationship between PoS and PoS_{post}

$$\begin{aligned}
 PoS_{post} &= \int P(\hat{\theta}_{fin} > \theta_{suc} | \theta_{fut} \leq \hat{\theta}_{int} \leq \theta_{eff}, \theta) q_1(\theta) d\theta \\
 &= \int \frac{P(\theta_{fut} \leq \hat{\theta}_{int} \leq \theta_{eff}, \hat{\theta}_{fin} > \theta_{suc} | \theta)}{\cancel{P(\theta_{fut} \leq \hat{\theta}_{int} \leq \theta_{eff} | \theta)}} \frac{P(\theta_{fut} \leq \hat{\theta}_{int} \leq \theta_{eff} | \theta) q_0(\theta)}{\int P(\theta_{fut} \leq \hat{\theta}_{int} \leq \theta_{eff} | \theta') q_0(\theta') d\theta'} d\theta \\
 &= \frac{P(\text{no early stop and success at final analysis})}{P(\text{no early stop})} \\
 &= \frac{PoS - P(\text{early stop for efficacy})}{P(\text{no early stop})}
 \end{aligned}$$

Fictive case study

Parallel group trial (2 arms: T and R)

Continuous response (treatment effect assessed as mean difference T vs. R)

Power = 0.9

Alpha = 0.025 (one-sided)

Standardized treatment effect of interest $\Delta = 0.3$

PoS is evaluated over 3 different priors of the form $\theta \sim \mathcal{N}\left(\theta_0, \frac{2}{n_0}\right)$

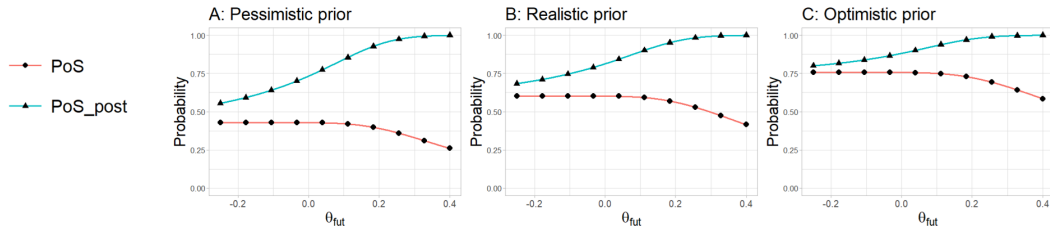
$$n_0 = 10$$

Pessimistic	Realistic	Optimistic
$\theta_0 = \Delta - 0.2$	$\theta_0 = \Delta$	$\theta_0 = \Delta + 0.2$

Case with no early stop for efficacy ($\theta_{eff} = +\infty$)

Tradeoff in the choice of the futility boundary: $\theta_{fut} \nearrow \implies \begin{matrix} PoS \searrow \\ PoS_{post} \nearrow \end{matrix}$

No early stop for efficacy

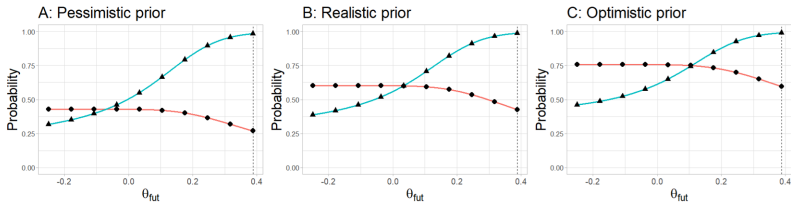


$$PoS_{post} = \frac{PoS}{P(\text{no early stop})} \implies PoS_{post} > PoS \quad (\text{not true for } \theta_{eff} < +\infty)$$

Case with an efficacy boundary

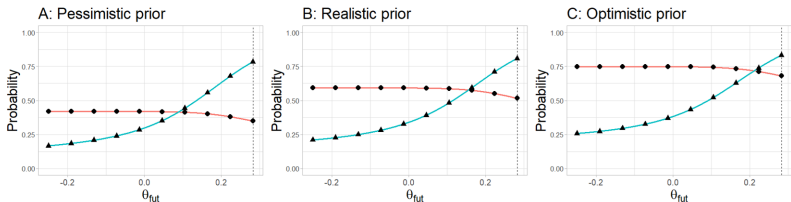
O'Brien-Fleming efficacy boundary

● PoS
▲ PoS_{post}



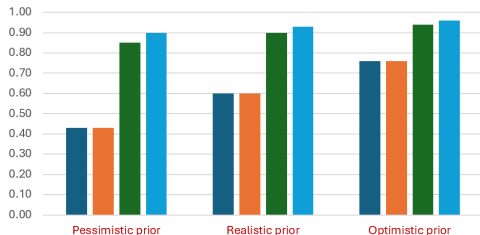
For some values of θ_{fut} ,
 $PoS_{post} < PoS$

Pocock efficacy boundary



PoS and PoS_{post} trade-off

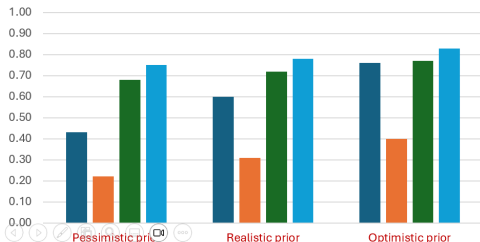
No early stop for efficacy



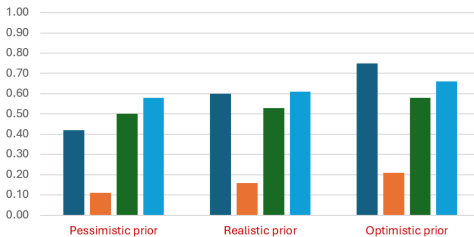
PoS reduced by a small amount with θ_{fut}
 $\Rightarrow PoS_{post}$ increased by a large amount

■ PoS without futility ■ PoS_post without futility
 ■ PoS_post when PoS is reduced by 0.01 ■ PoS_post when PoS is reduced by 0.02

O'Brien-Fleming efficacy boundary



Pocock efficacy boundary



Take-home messages

With an efficacy stopping rule, continuing after the interim may reduce the probability of success.

Tradeoff in the choice of the futility boundary: $\theta_{fut} \nearrow \Rightarrow \begin{matrix} PoS \searrow \\ PoS_{post} \nearrow \end{matrix}$

An appropriate choice of θ_{fut} may lead to a significantly larger PoS_{post} , with minimal losses in PoS .

Some reference

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